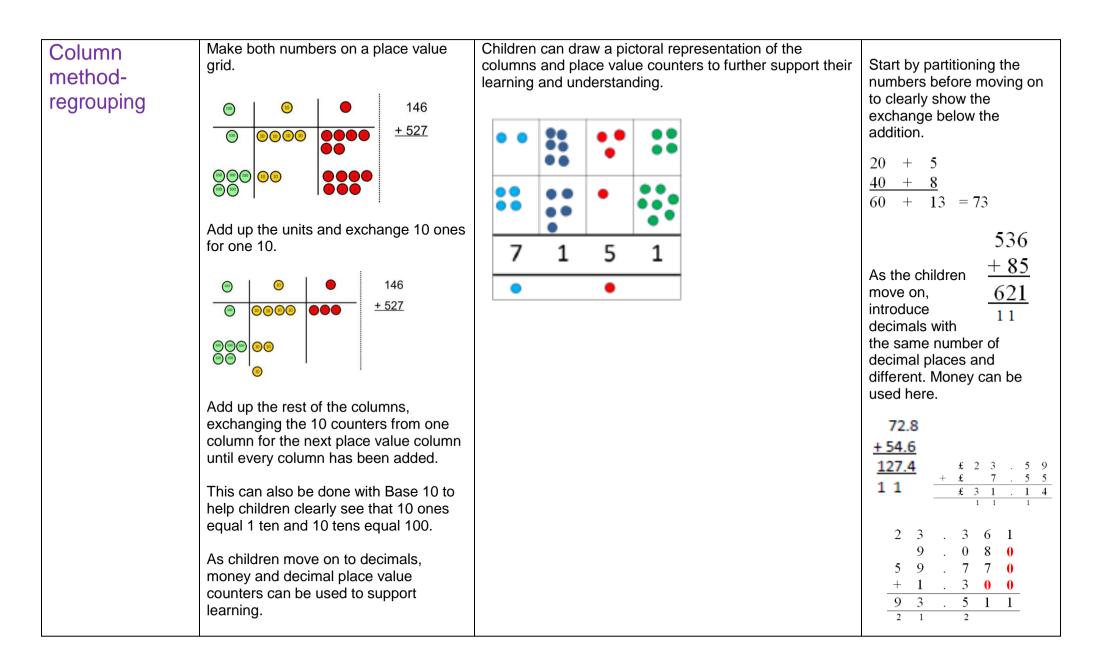
## Progression in Calculations

### Addition

Objective and Strategies	Concrete	Pictorial	Abstract
Combining two parts to make a whole: part- whole model	Use cubes to add two numbers together as a group or in a bar.	3       3	4 + 3 = 7 $10 = 6 + 4$ $3$ Use the part-part whole diagram as shown above to move into the abstract.
Starting at the bigger number and counting on	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	12 + 5 = 17 $+ + + + + + + + + + + + + + + + + + +$	5 + 12 = 17 Place the larger number in your head and count on the smaller number to find your answer.

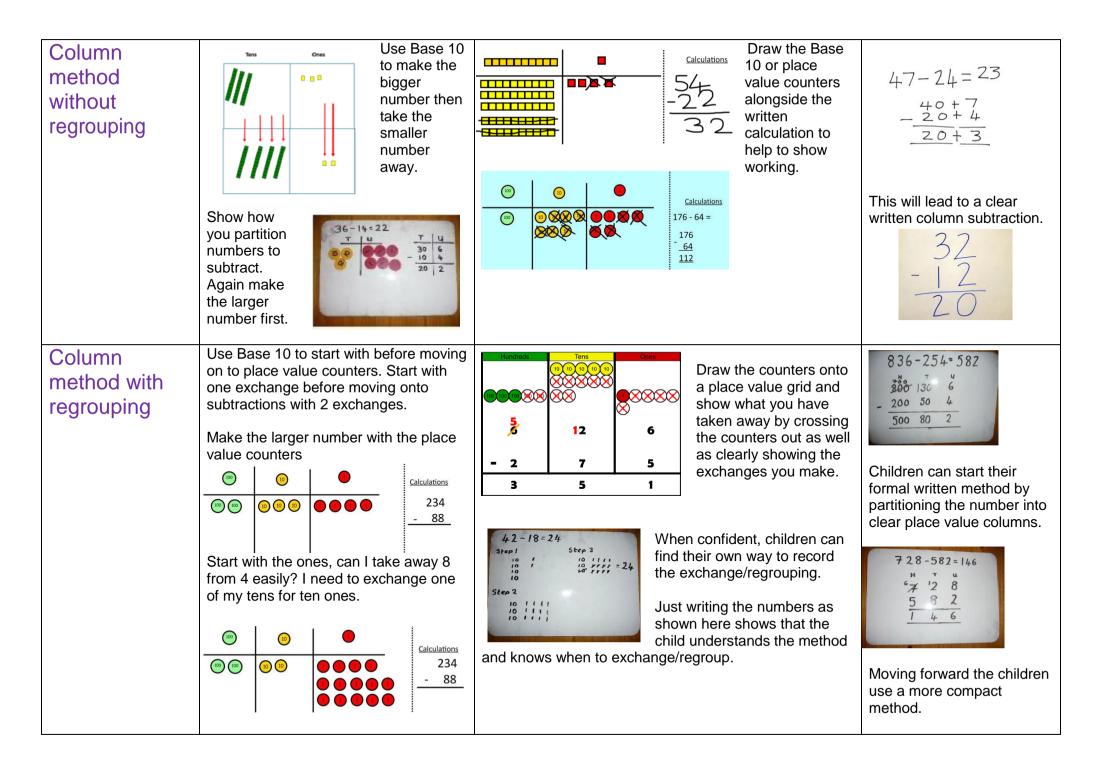
Regrouping to make 10.	6 + 5 = 11	Use pictures or a number line. Regroup or partition the smaller number to make 10.	7 + 4= 11 If I am at seven, how many more do I need to make 10. How many more do I add on now?
	Start with the bigger number and use the smaller number to make 10.	9 + 5 = 14 $+1$ $+1$ $+1$ $+1$ $+1$ $+1$ $+1$ $+1$	
Adding three single digits	4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7.		4 + 7 + 6 = 10 + 7 $= 17$ Combine the two numbers that make 10 and then add on the remainder.
	Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	Add together three groups of objects. Draw a picture to recombine the groups to make 10.	
Column method- no regrouping	24 + 15= Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters. T O O O O O O O O O O O O O O O O O O	After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions.	$\frac{Calculations}{21 + 42} = \frac{21}{42} + \frac{42}{42}$

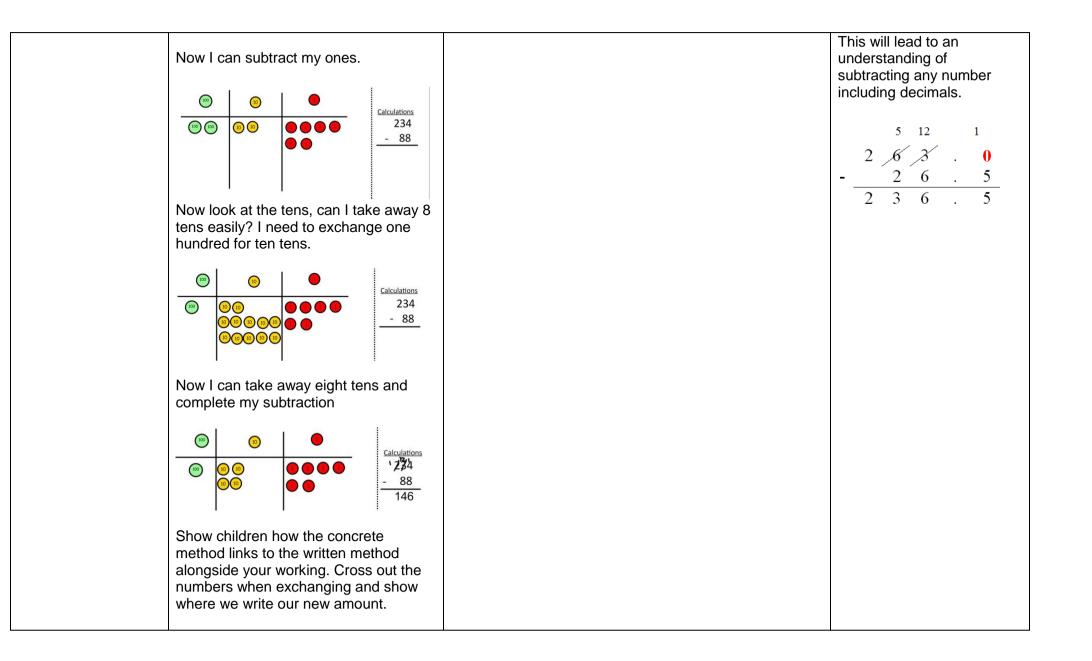


#### Subtraction

Objective and Strategies	Concrete	Pictorial	Abstract
Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away. 6-2=4	Cross out drawn objects to show what has been taken away. $\begin{array}{c} & & & & \\ & & & & \\ & & & & \\ & & & & $	18 -3= 15 8 - 2 = 6
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. 13 – 4 Use counters and move them away from the group as you take them away counting backwards as you go.	Count back on a number line or number track 9 10 11 12 13 14 15 Start at the bigger number and count back the smaller number showing the jumps on the number line. -10 -10 -10 -10 -10 -10 -10 -10 -10 -10	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.

Find the difference	Compare amounts and objects to find the difference. Use cubes to build towers or make bars to find the	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	Hannah has 23 sandwiches, Helen has 15 sandwiches. Find the difference between the number of sandwiches.
	12 difference       S Pencils     Use basic bar models with items to find the difference       3 Erasers     2	Draw bars to find the difference between 2 numbers.	
Part Part Whole Model	Link to addition- use the part whole model to help explain the inverse between addition and subtraction. If 10 is the whole and 6 is one of the parts. What is the other part? 10 - 6 =	Use a pictorial representation of objects to show the part part whole model.	5 10 Move to using numbers within the part whole model.
Make 10	14 – 9 = Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9.	13 - 7 = 6 3 4 - 3 - 4 - 3 - 3 - 4 - 3 - 5 - 6 - 7 - 18 - 19 20 - 4 - 15 - 16 - 17 - 18 - 19 20 - 4 - 15 - 16 - 17 - 18 - 19 20 - 4 - 15 - 16 - 17 - 18 - 19 20 - 4 - 15 - 16 - 17 - 18 - 19 20 - 4 - 15 - 16 - 17 - 18 - 19 20 - 4 - 15 - 16 - 17 - 18 - 19 20 - 4 - 15 - 16 - 17 - 18 - 19 20 - 4 - 15 - 16 - 17 - 18 - 19 20 - 4 - 19 20 - 5 - 19 20 - 7 - 19 20	16 – 8= How many do we take off to reach the next 10? How many do we have left to take off?





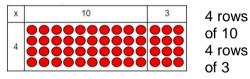
### **Multiplication**

Objective and Strategies	Concrete	Pictorial	Abstract
Doubling	Use practical activities to show how to double a number.	Draw pictures to show how to double a number. Double 4 is 8	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
Counting in multiples	Count in multiples supported by concrete objects in equal groups.	Use a number line or pictures to continue support in counting in multiples.	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30

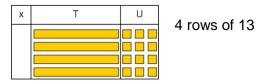
Repeated	3 + 3 + 3         Use different objects to add equal groups.	There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?	Write addition sentences to describe objects and pictures.
addition		$ \begin{array}{c}  \end{array} $ $ \end{array} $ $ \end{array} $ $ \begin{array}{c}  \end{array} $ $ \end{array} $ $ \end{array} $ $ \end{array} $	2+2+2+2+2=10
Arrays- showing commutative multiplication	Create arrays using counters/ cubes to show multiplication sentences.	Draw arrays in different rotations to find <b>commutative</b> multiplication sentences.	Use an array to write multiplication sentences and reinforce repeated addition. 000000000000000000000000000000000000

#### **Grid Method**

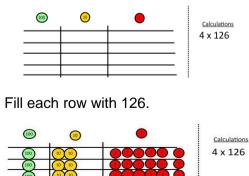
# Show the link with arrays to first introduce the grid method.



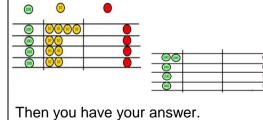
Move on to using Base 10 to move towards a more compact method.



Move on to place value counters to show how we are finding groups of a number.We are multiplying by 4 so we need 4 rows.

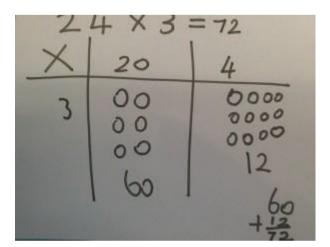


Add up each column, starting with the ones making any exchanges needed.



Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.



Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

×	30	5
7	210	35

210 + 35 = 245

Moving forward, multiply by a 2 digit number showing the different rows within the grid method.

	10	8
10	100	80
3	30	24

Х	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16

Column multiplication	Children can continue to be supported by place value counters at the stage of multiplication.	Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.	Start with long multiplication, reminding the children about lining up their numbers clearly in columns.
	6° 3 64×3 = 192	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	If it helps, children can write out what they are solving next to their answer.
	It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below.	250ml 3 - 250ml 4 - 250ml	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
		4 + 4 + 8 + 8 + 16 5 * 8 = 40 jugs-	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
			This moves to the more compact method.
			1342
			x 18
			13420
			10736
			24156

# **Division**

Objective and Strategies	Concrete	Pictorial	Abstract
Sharing objects into groups	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. 32 $32$ $32$ $32$ $32$ $32$ $32$ $32$	Share 9 buns between three people. $9 \div 3 = 3$
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use a number line to show jumps in groups. The number of jumps equals the number of groups. 0 1 2 3 4 5 6 7 8 9 10 11 12 3 3 3 3 3 3	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.	
		20 ? 20 ÷ 5 = ? 5 x ? = 20	

Division within arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$	Image: Constraint of the series of the se	Find the inverse of multiplication and division sentences by creating four linking number sentences. 7 x 4 = 28 4 x 7 = 28 28 $\div$ 7 = 4 28 $\div$ 4 = 7
Division with a remainder	14 ÷ 3 = Divide objects between groups and see how much is left over	Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder. 0 4 8 12 13 Draw dots and group them to divide an amount and clearly show a remainder. () () () () () () () () () () () () () (	Complete written divisions and show the remainder using r. $29 \div 8 = 3 \text{ REMAINDER 5}$ $\uparrow \uparrow \uparrow \uparrow \uparrow$ dividend divisor quotient remainder

